ST(+) dt= (Same dt, Sycholt, SzG+) dt)

+=a

, Same dt, Sycholt, SzG+) dt) four space curve T.Ct) = (xCt), yCt), zCt)7 The one length of a curre should be computable by I approximate curve by streight his regenerality af curve. limit these , using were and were him reggments 9/17/202 Ex: Compute the tangent line for f(+)= <2cos(+), 2sin(+), 4cos(at (\sqrt{3},1,2). Sol: F(+) = <-2 sin (m+), 2 cos (m+), -8 sin (2+)); Nead + for the point ($\sqrt{3}$, 1, 2), $2 \cos(t) = \sqrt{3}$, $\cos(t) = \sqrt{3}/2$; $1 = \frac{\pi}{6} + 2K\pi$ $2 \sin(t) = 1 = 1$ $\sin(t) = 1/2$ Check: $(2 \cdot \frac{\pi}{6}) = \cos(\frac{\pi}{3}) = \frac{1}{2}$ $1 \cos(2t) = 1/2$ Cos (2t) = 1/2 Cos (The tangent vector at the point given is $T'(\pi/6) = \langle -2\sin(\frac{7}{3}), 2\cos(\frac{\pi}{3}), -8\sin(\frac{2\pi}{6}) \rangle$ $= \langle -1, \sqrt{3}, -4\sqrt{3} \rangle$.. The tangent has vector equation. u(+) = P++r'(7/2) = (13,1,2)++<-1,13,-4/37 2 (13-1, 1+13+, 2-4, 3+)

Section: 13. Arc length.

Recall: the are length of space curve
$$F(t)$$
 between times $t=a$ and b is

 $S = \int_{0}^{b} |\overline{r}'(t)| dt$
 $t=a$
 $\overline{r}(t)$ is a space curve in \mathbb{R}^{3} : $\overline{r}(t) = \langle x(t), y(t) \rangle$
 $|\overline{r}'(t)| = \langle x'(t), y'(t) \rangle$

for a plane curve (like in Calc II)

arc $S = \int_{0}^{b} |\overline{dx}|^{2} + |\overline{dy}|^{2} dt$
 $|\overline{r}(t)| = \int_{0}^{b} |\overline{dx}|^{2} + |\overline{dx}|^{2} dt$
 $|\overline{r}(t)| = \int_{0}^{b} |\overline{r}(t)|^{2} + |\overline{r}(t)|^{2} + |\overline{r}'(t)|^{2} + |\overline{r}'(t)$

$$|\vec{r}'(t)|^{2} = \sqrt{(-\sin(t))^{2} + (\cos(t))^{2} + (-\tan(t))^{2}}$$

$$= \sqrt{\sin^{2}(t) + (\cos^{2}(t))^{2} + (-\tan(t))^{2}}$$

$$= \sqrt{1 + \tan^{2}(t)}.$$

=
$$\sqrt{\sec^2(4)}$$
 = $|\sec(4)|$ = $\sec(4)$ on $0 \le 1 \le \frac{91}{4}$



Finally:
$$S = \frac{1}{2} \int_{Sec}^{\infty} (\theta) d\theta$$
 $f = \frac{\pi}{3}$
 $f = \frac{1}{4} [\ln |\sec(\theta)| + \tan(\theta)| + \sec(\theta) + \tan(\theta)| + \frac{\pi}{3}$
 $f = \frac{1}{4} [\ln |\sqrt{1+q+2}| + 2+| + \sqrt{1+q+2}| + \frac{\pi}{3}$
 $f = \frac{1}{4} [\ln |\sqrt{1+q+2}| + 2\pi |+ 2\pi |+ 4\pi^2| + \frac{\pi}{3}$

The are length is the most natural parameter for a curve.

In particular if we make a parameter zation of the curve with arc length s at time s (measured from the paint), then that parameter zation has curve speed.

From the parameter zation has curve speed.